

# Chemical control of polar behavior in bicomponent short-period superlattices

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Using first-principles density functional calculations, we study the interplay of ferroelectricity and polar discontinuities in a range of 1–1 oxide superlattices, built out of ferroelectric and paraelectric components. Studies have been carried out for a varied choice of chemical composition of the components. We find that, when polar interfaces are present, the polar discontinuities induce off-centric movements in the ferroelectric layers, even though the ferroelectric is only one unit cell thick. The distortions yield nonswitchable polarizations, with magnitudes comparable to those of the corresponding bulk ferroelectrics. In contrast, in superlattices with no polar discontinuity at the interfaces, the off-centric movements in the ferroelectric layer are usually suppressed. The details of the behavior and functional properties are, however, found to be sensitive to epitaxial strain, rotational instabilities and second-order Jahn-Teller activity, and are therefore strongly influenced by the chemical composition of the paraelectric layer.

## I. INTRODUCTION

Superlattices formed by layer-by-layer epitaxial growth of perovskite-based oxide materials are currently a subject of intense research, because of their promising technological applications as well as fundamental scientific interest.<sup>1</sup> In ABO<sub>3</sub> perovskites, the A<sup>+2</sup>B<sup>+4</sup>O<sub>3</sub> (II-IV) structures consist of (100) layers of formally charge neutral AO and BO<sub>2</sub>, while A<sup>+3</sup>B<sup>+3</sup>O<sub>3</sub> (III-III) or A<sup>+1</sup>B<sup>+5</sup>O<sub>3</sub> (I-V) structures have charged planes, composed of +1 AO and –1 BO<sub>2</sub> layers or –1 AO and +1 BO<sub>2</sub> layers, respectively. By stacking two perovskite layers from different charge families along the [001] direction, one obtains a *polar discontinuity* at the interface. Such polar discontinuities have been reported to lead to nontrivial local structural and electronic ground states,<sup>2–5</sup> which are often not present in the parent bulk compounds.<sup>1,6,7</sup> Investigating the properties of these “exotic” local phases has been an increasingly active area of research in the past few years, particularly following a 2004 report<sup>2</sup> of a conducting quasi-two-dimensional electron gas (2DEG) at the interface between two wide-band insulators, LaAlO<sub>3</sub> (LAO) and SrTiO<sub>3</sub> (STO). The measured mobility and carrier density of the LAO/STO interface are an order of magnitude larger than those in analogous semiconductor-based systems.<sup>8</sup> Furthermore, magnetism,<sup>3</sup> superconductivity<sup>4</sup> and a rich electronic phase diagram<sup>5</sup> have also been reported for this same system. These fascinating and unexpected effects have generated strong excitement, and an intense effort is currently devoted to better understanding the fundamental mechanisms of charge compensation at polar oxide-oxide interfaces. Parallel to this thrust, from the materials-design point of view, it is also important to identify new compounds, artificial superlattices or interfaces that might display similar (or possibly even more striking) behavior.

A system can respond in several different ways to avoid a so-called *polar catastrophe*<sup>9</sup>—a divergence in the potential caused by the polar discontinuity—at such an interface between two charge-mismatched perovskites. Compensation by

free carriers was proposed in Ref. 2, and is consistent with the observed conductivity at the interfaces. Other likely possibilities are direct ionic charge compensation through mixed valency of the B cation, ion intermixing or oxygen vacancies at the interface,<sup>10</sup> or polar distortions at the interface. These can be “induced” by the polar discontinuity if both materials are paraelectric (PE) in their bulk phase,<sup>11</sup> or “natural” if one or both components in the superlattice is ferroelectric (FE).<sup>12</sup>

The mechanisms underlying induced and natural polar distortions can be readily understood in terms of classical electrostatics and the modern theory of polarization,<sup>13</sup> whenever the relevant layers in the superlattice are at least three or four unit cells thick. In particular, the charge mismatch can be interpreted as a polarization discontinuity, which produces macroscopic electric fields in one or both components, because the normal component of the electric displacement field,  $D = \mathcal{E} + 4\pi P$ , is preserved at a coherent insulating interface. For smaller thicknesses, macroscopic concepts lose their meaning, as each film is too thin to identify a well-defined local value of the electric field or the polarization. Thus, it remains an important question whether the above concepts are still valid when the layers in a superlattice are made thinner and thinner, down to the ultrathin extreme limit of a single unit cell, or whether new phenomena arise that radically alter the physics. It is the main scope of this work to answer this question by studying some computer designed examples of 1–1 superlattices, constructed out of ferroelectric and paraelectric layers, with different composition and choices of polar/nonpolar combinations. We stress that this question has some points of contact with, but is largely unrelated to the better-known problem of the critical thickness for ferroelectricity<sup>14</sup> since the present problem deals with nonswitchable polar distortions driven by a polar discontinuity rather than switchable ferroelectric behavior.

In addition to issues related to the presence or absence of a polar discontinuity, other factors can influence or complicate the properties of the 1–1 bicomponent superlattices. In particular, structural instabilities such as the rotation and tilting of oxygen octahedra, the presence of misfit strain, and

the presence of  $d^0$  ions—associated with a tendency to ferroelectricity—in otherwise paraelectric layers, are likely to strongly affect the behavior. It is therefore of interest to study how these additional factors may alter the properties of the short-period superlattices compared to those expected solely out of consideration of the presence or absence of a polar discontinuity.

To separate the role of electrostatics from the role of the specific choice of cations within a given charge family, we investigate bicomponent superlattices with alternating III-III/II-IV and I-V/II-IV perovskite layers (with interfacial polar discontinuities), as well as others with alternating II-IV/II-IV and I-V/I-V perovskite layers (without polar discontinuities), both for a variety of chemical constituents. We find that our 1–1 structures behave in a way which is qualitatively analogous to the longer-period superlattices previously investigated in the literature. In particular, the systems containing polar discontinuities have strongly broken inversion symmetry and large polarizations, but are not switchable. The magnitudes of the polar distortions are as large as those in the corresponding bulk FE materials. The superlattices formed out of PE and FE layers with no potential discontinuity at the interface, on the other hand, usually have their off-centric displacements suppressed. We do, however, find examples of superlattices without polar mismatch that show marked ferroelectric instability, driven by either suppression of rotational instability or due to the presence of  $d^0$  ions in the PE layer.

The remainder of the paper is organized as follows. Section II includes the methodology and the details of the computations carried out in this study. In Sec. III we present our results and discussion in several subsections dealing, respectively, with the bulk properties of the constituent materials, the calculated structural properties of the superlattices (with and without polar discontinuities), and the calculated functional properties including static dielectric constants. Section IV provides the summary.

## II. METHODOLOGY AND COMPUTATIONAL DETAILS

Our calculations are performed using the plane wave based pseudopotential framework of density functional theory (DFT) (Refs. 15 and 16) as implemented in the Vienna *ab initio* Simulation Package (VASP).<sup>17,18</sup> We choose the local density approximation (LDA) rather than generalized gradient approximation (GGA) to describe the exchange-correlation functional due to the later’s systematic overestimation of polar behavior.<sup>19</sup> The optimized geometries are obtained by full relaxation of the atomic positions and out-of-plane lattice constants ( $c$ ), with the in-plane lattice constants ( $a$ ) fixed to the LDA bulk lattice constant of the ferroelectric component in the tetragonal phase, which would impose appropriate strains, as discussed later. The positions of the ions are relaxed toward equilibrium until the Hellmann-Feynman forces become less than 0.001 eV/Å. A  $4 \times 4 \times 4$  Monkhorst-Pack  $k$ -point mesh<sup>20</sup> and 450 eV plane-wave cutoff give good convergence of the computed ground-state properties.

The Born effective charges, phonon frequencies and dielectric tensors are obtained from linear response

TABLE I. Representative bicomponent superlattices composed of paraelectric (PE) and ferroelectric (FE) components.

	PE	FE	Polar interface?	Mismatch (%)
LAO/PTO	LaAlO <sub>3</sub>	PbTiO <sub>3</sub>	YES	0.99
KSO/PTO	KSbO <sub>3</sub>	PbTiO <sub>3</sub>	YES	1.94
KSO/KNO	KSbO <sub>3</sub>	KNbO <sub>3</sub>	NO	0.10
SSO/PTO	SrSnO <sub>3</sub>	PbTiO <sub>3</sub>	NO	4.40

calculations,<sup>21</sup> using a variational formalism<sup>22</sup> of the density functional perturbation theory, as implemented in the ABINIT code. We calculate the electronic contribution to the polarization as a Berry phase using the method developed by King-Smith and Vanderbilt,<sup>23</sup> and extract the ionic contribution by summing the product of the position of each ion with its pseudocharge.

The first part of our study concerns superlattices formed by alternating FE and PE single simple perovskite unit cells in the  $z$  direction, and constraining them to be tetragonal in the  $x$ - $y$  plane. In a second stage, we consider structures formed by alternating  $2 \times 2 \times 2$  PE and FE cubic perovskite unit cells to allow rotation and tilting of the BO<sub>6</sub> octahedra.

## III. RESULTS AND DISCUSSION

We consider the four representative systems listed in Table I. All combinations contain one material which is ferroelectric in the bulk, and one which is paraelectric. Two of the systems (LAO/PTO and KSO/PTO) have polar discontinuities at the interface whereas the other two (KSO/KNO and SSO/PTO) do not. We deliberately choose paraelectric components without  $d^0$  cations, because  $d^0$  cations have a strong tendency to off-center through the so-called second-order Jahn-Teller effect. This often results in ferroelectricity, and in materials with paraelectric ground states it can cause incipient or quantum ferroelectricity,<sup>24</sup> which we choose to avoid here. We begin by briefly summarizing the relevant bulk properties of the various constituents.

### A. Bulk properties

Both PTO and KNO are well-known ferroelectric materials with the cubic perovskite structure at high temperature. PTO undergoes a phase transition to a tetragonal phase below 766 K, with the polarization along the [001] direction. In the tetragonal phase the experimental in-plane ( $a$ ) and out-of-plane ( $c$ ) lattice parameters are 3.90 and 4.14 Å, respectively,<sup>25</sup> and the ferroelectric polarization is 59  $\mu\text{C}/\text{cm}^2$ ; our calculated corresponding LDA values are 3.85 and 4.05 Å, and 80.45  $\mu\text{C}/\text{cm}^2$ , respectively. Bulk KNO is a rhombohedral ferroelectric with a polarization of 42  $\mu\text{C}/\text{cm}^2$  along [111] below its Curie temperature<sup>26</sup> of 230 K. Earlier theoretical work reported stabilization of the tetragonal phase with compressive strain;<sup>27</sup> for tetragonal KNO we obtain in- and out-of-plane lattice constants of 3.92 and 4.00 Å and a polarization of 26  $\mu\text{C}/\text{cm}^2$  along [001].

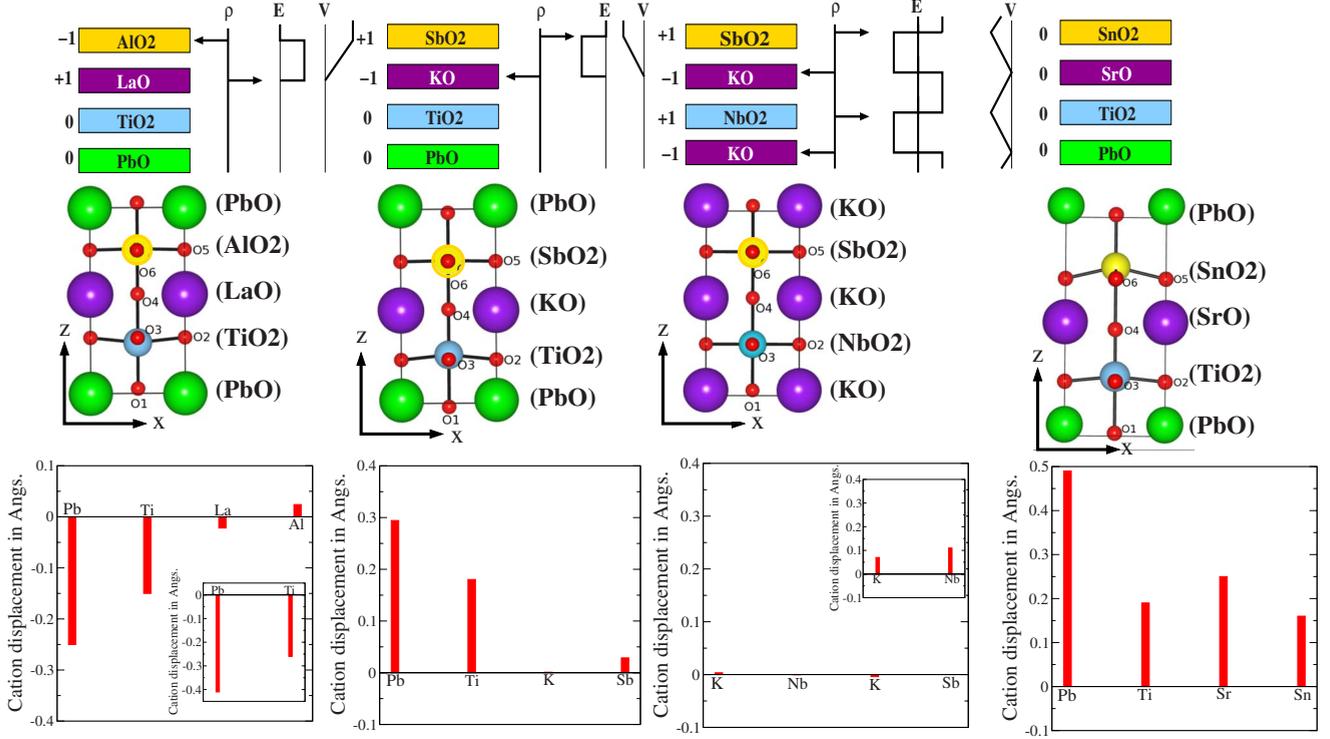


FIG. 1. (Color online) Upper panel: Polar catastrophe for atomically abrupt (001) interfaces between LAO and PTO, KSO and PTO, KSO and KNO, SSO and PTO (left to right). The charges of each AO and BO<sub>2</sub> layer are taken from the formal charges of the constituent ions, after Ref. 2. Middle panel: Optimized structures for LAO/PTO, KSO/PTO, KSO/KNO and SSO/PTO, projected onto the *xz* plane. The large spheres indicate the cations at various layers, while the small spheres indicate oxygens. Inequivalent oxygens are indicated. Lower panel: Cation displacements along the *z* axis, with respect to the centers of their oxygen cages. The insets show the displacements for corresponding bulk FE's.

LAO is a wide band gap insulator with strong alternating rotations of the oxygen octahedra around the [111] direction leading to rhombohedral symmetry.<sup>28</sup> Recent density functional calculations showed that epitaxial strain causes a polar instability which competes with these nonpolar oxygen rotations.<sup>29</sup> The lattice parameter for the cubic structure without oxygen rotations is 3.81 Å.<sup>28</sup> KSO is not known experimentally. Computationally we obtain a cubic LDA optimized lattice constant of 3.92 Å. At room temperature SSO crystallizes in the centrosymmetric orthorhombic space group *Pbnm*,<sup>30</sup> with lattice parameters  $a=5.71$  Å,  $b=5.71$  Å, and  $c=8.06$  Å. The structure is characterized by a classic GdFeO<sub>3</sub> tilt pattern of the SnO<sub>6</sub> octahedra. A structural transition from the ground-state orthorhombic structure to a high temperature tetragonal *I4/mcm* phase has been found<sup>31</sup> driven by an order-disorder octahedral tilting transition.

## B. Structural properties

We begin by optimizing the geometries of our four representative superlattices. We construct the superlattices by alternating FE and PE layers along the [001] direction. We impose an in-plane periodicity of one simple cubic perovskite unit cell: This choice imposes an overall tetragonal symmetry and prohibits rotations and tiltings of the oxygen octahedra. We investigate the effects of relaxing this constraint later. By fixing the in-plane lattice constant to the

LDA value for the FE layer we induce a small tensile strain in the PE layer for LAO on PTO, small compressive strains for KSO on PTO or KNO, and a large compressive strain for SSO on PTO (values in Table I). We then fully relax the out-of-plane lattice parameter and the ionic positions within the tetragonal symmetry. All superlattices are found to be insulating within the LDA with band gaps of  $\sim 2$  eV, allowing us to directly calculate their ferroelectric polarization using the Berry phase formalism.<sup>23</sup>

Both superlattices containing polar discontinuities are strongly polar, with polarizations of  $-50.87$   $\mu\text{C}/\text{cm}^2$  for LAO/PTO and  $+57.74$   $\mu\text{C}/\text{cm}^2$  for KSO/PTO; the opposite signs in the two cases reflect the opposite orientation of the polar discontinuity (III-III/II-IV in the first case and I-V/II-IV in the second). Neither case is ferroelectric, because the polarization orientations are fixed by the polar discontinuity and the polarizations are not switchable.<sup>12</sup> The calculated structures are shown in Fig. 1. In LAO/PTO, the Pb and Ti ions displace from the centers of their coordination polyhedra by  $\approx 0.25$  and  $0.15$  Å, respectively, along the positive crystallographic *z* axis, that is toward the PbO/AIO<sub>2</sub> interface. In KSO/PTO, Pb and Ti off-center by  $0.29$  and  $0.18$  Å, respectively, along the negative *z* axis, away from the PbO/SbO<sub>2</sub> interface. The magnitudes of these displacements are similar to those in bulk PTO, which are  $0.41$  and  $0.26$  Å for Pb and Ti, respectively (see insets in lower panel of Fig. 1). Note that the off-centric movements in the LaO/KO and AIO<sub>2</sub>/SbO<sub>2</sub> layers are tiny, with the movements of K and Sb

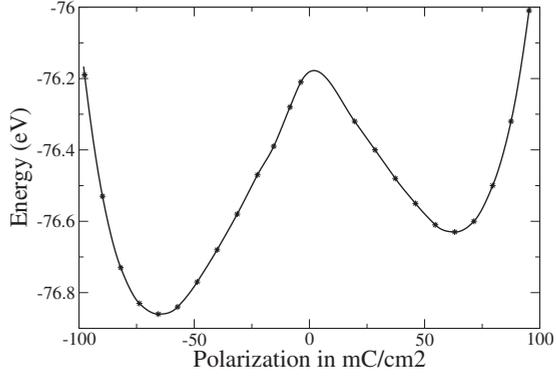


FIG. 2. Potential energy curve of the total polarization for SSO/PTO superstructure for  $1 \times 1 \times 1 / 1 \times 1 \times 1$  geometry (see text for details).

(antimony) being in the same direction as Pb and Ti, and La and Al moving in the opposite direction to each other. We, however, do not attach much significance to these small displacements.

The situation for the superlattices without polar discontinuities is more complicated. For KSO/KNO we indeed obtain a negligible polarization of  $0.02 \mu\text{C}/\text{cm}^2$ , resulting from the tiny displacements of K and Nb from the centers of their coordination polyhedra.<sup>32</sup> Note that the KSO/KNO superlattice in its paraelectric phase has an inversion center. However we do not impose the inversion symmetry during the relaxation procedure, since our aim is to find out the existence or nonexistence of the polar behavior. The tiny polarization obtained for relaxed geometry of KSO/KNO is within the accuracy limit of our calculations. This leads us to conclude that our obtained geometry is in fact centrosymmetric, as has been checked in terms of the energy difference between the fully centrosymmetric case and the relaxed structure, which turned out to be less than  $0.01 \text{ meV}$ . For SSO/PTO, however, we obtain a rather large polarization of  $\sim -66 \mu\text{C}/\text{cm}^2$ , with a cooperative displacement of all cations (Sr, Sn, Pb, Ti). Interestingly, the polarization is found to be switchable: In Fig. 2 we show the calculated total energy,  $E$  as a function of polarization  $P$  obtained by calculating polarizations and total energies of geometries with fixed values of off-centric movements. The fixed values of off-centric movements are obtained by interpolating between off-centric movements of ions corresponding to two minima of the  $E$  versus  $P$  curve. The  $E(P)$  curve shows the characteristic double well structure typical of switchable ferroelectrics, except that in this case it is strongly asymmetric as a result of the additional inversion-center lifting that is built in to the structure through the layering. The switchable behavior indicates that the polarization arises from an origin other than the polar discontinuity alone, as the polar discontinuity can only drive the polarization in one direction. Note that it is also likely distinct from the behavior in  $\text{BaTiO}_3/\text{SrTiO}_3$  superlattices<sup>33</sup> where the PE component (STO) is a quantum ferroelectric. In the next section we explore the origin of this behavior.

### C. Origin of polarization at nonpolar interfaces

Our first clue as to the origin of the unexpected polarization in the SSO/PTO superlattice lies in the large (4.4%)

mismatch in lattice constants between the two constituents in this system. To test the role of the misfit strain in driving polarization, we performed an analogous set of calculations for  $\text{SrSnO}_3/\text{BaTiO}_3$  (SSO/BTO), in which the misfit strain (estimated using the experimental bulk lattice constants<sup>34,35</sup>) is only 0.78%. Indeed, we find that the calculated polarization for SSO/BTO is considerably reduced (to  $-7.76 \mu\text{C}/\text{cm}^2$ ) compared with SSO/PTO, and the corresponding off-center displacements are 0.02, 0.06, 0.06, and  $0.02 \text{ \AA}$  for Sr, Sn, Ba, and Ti, respectively. We have further carried out calculations for bulk  $\text{SrSnO}_3$  in tetragonal geometry, disabling the rotation and tilt of the  $\text{SnO}_6$  octahedra, under 4.4% and 0.78% compressive strains (strains identical to SSO/PTO and SSO/BTO systems, respectively). These calculations resulted in large off-centric displacements of  $\text{Sr}^{2+}$  and  $\text{Sn}^{4+}$  ions for 4.4% compression strain and negligible displacements for 0.78% strain value, illustrating once more the essential role of the strain in determining the polarization.

While it is an already established result<sup>36</sup> that strain plays a crucial role in determining polarization and off-centering in superlattices, there has also been recent discussion of competition between tilts and rotations of the oxygen octahedra and ferroelectric displacements. For example it has been shown computationally<sup>29</sup> that  $\text{LaAlO}_3$  shows ferroelectric behavior under epitaxial strain when the octahedral rotations are suppressed, while ferroelectricity is suppressed when those rotations are allowed to relax.<sup>29</sup> Similar physics led to predictions of ferroelectricity in A-site alloy perovskites,<sup>37</sup> in which the polar behavior is obtained by destabilizing the cooperative rotational instability through A-site disorder. And in Ref. 38, polar behavior was engineered theoretically in  $\text{CaMnO}_3$  by suppressing the orthorhombic tilting instability through strain and chemical substitution. The possibility of competing rotational instability governed by zone-boundary phonons with ferroelectric modes should therefore be carefully analyzed before drawing a definitive conclusion on a specific system.

To check for this possibility in our superlattices, we increased the size of our supercell to  $2 \times 2 \times 2$  simple perovskite unit cubes in order to allow for oxygen rotations and tiltings and recompute the lowest energy structures. Indeed we find that, while for LAO/PTO, KSO/PTO, and KSO/KNO our conclusions remain unchanged, for SSO/PTO the system adopts a centrosymmetric structure with negligible off-centering when rotational distortions are allowed. Bulk  $\text{SrSnO}_3$  calculations allowing for the octahedral rotation and tilt, as expected, also yielded a centrosymmetric structure. We find applied compressive strain increases the rotation and decreases the tilt in agreement with the findings in Ref. 29. This reinforces the earlier suggestions in the literature, and implies that if octahedral rotation at the SSO layer can be disabled, which might be possible in ultrathin films using strain or doping, then SSO/PTO superlattices could have switchable polar properties.

### D. Ferroelectric tendency in the paraelectric layer

In all of the model superlattices studied above, the paraelectric material was chosen to be one that shows no

tendency to ferroelectric off-centering in its bulk phase. In this section we study the effect of substituting it with an “incipient ferroelectric” or “quantum ferroelectric,” i.e., a material that is still PE in the bulk, but very close to a ferroelectric phase transition.

Specifically we compare our results reported above for KSO/KNO with analogous calculations for  $\text{KTaO}_3/\text{KNbO}_3$  1–1 superlattices. We choose  $\text{KTaO}_3$  to compare with  $\text{KSbO}_3$  because the former has a so-called second-order Jahn-Teller (SOJT) active<sup>39</sup> ion with a  $d^0$  electron configuration which is associated with a tendency to off-center. Indeed bulk KTO is a quantum ferroelectric with ferroelectricity suppressed by quantum fluctuations.<sup>24</sup> Ultrashort-period  $(\text{KTO})_m/\text{KNO}$  superlattices have been previously investigated<sup>40</sup> in terms of *ab initio* studies. As in Ref. 40 for  $m=1$ , we find that KTO/KNO is strongly ferroelectric, with a switchable polarization of  $16.46 \mu\text{C}/\text{cm}^2$  and atomic displacement at the Ta site of  $0.14 \text{ \AA}$ .

The difference in physical behavior between KTO/KNO and KSO/KNO must arise from the chemical difference between KTO and KSO. To further understand this, we next compute the Born effective charges,  $Z^*$  for KTO and KSO, using the  $c/a$  ratios that we obtained for the superlattice geometries. The Ta  $Z^*$  in KTO is highly anomalous (8.78 instead of the nominal valence of 5), consistent with the proximity of the  $d^0$  KTO system to ferroelectricity, while the Sb  $Z^*$  in KSO is 5.4, close to the nominal value of 5. The strong ferroelectric instability in KNO is therefore able to induce a ferroelectric instability in the proximally ferroelectric KTO layer; KSO is less polarizable and therefore resists polar distortion.

We also compute the properties of the  $\text{KTaO}_3/\text{PbTiO}_3$  superlattice in order to study the behavior of a ferroelectrically active paraelectric in a superlattice with a polar discontinuity. Here KTO is under 3.51% compressive strain. We find a nonswitchable polarization of  $69.72 \mu\text{C}/\text{cm}^2$  and displacements of 0.39, 0.26, 0.06, and  $0.10 \text{ \AA}$  for Pb, Ti, K, and Ta, respectively; all of these quantities are larger than the corresponding values for LAO/PTO and KSO/PTO, expected because in this case SOJT activity is additive with polar discontinuity behavior.

### E. Static dielectric constant

Finally, for completeness, we compute the dielectric properties of the polar PE-FE superlattices driven by polarization discontinuity, specifically LAO/PTO and KSO/PTO. Our motivation lies in the fact that the dielectric constants typically hold signatures of polar instability of soft modes<sup>41</sup> and are also of technological importance.

The  $\alpha\beta$  component of the static dielectric constant is given by

$$\epsilon_{\alpha\beta} = (\epsilon^\infty)_{\alpha\beta} + \frac{4\pi}{\Omega_0} \sum_{\omega_\mu^2 \neq 0} \frac{\bar{Z}_{\mu\alpha}^* \bar{Z}_{\mu\beta}^*}{\omega_\mu^2}, \quad (1)$$

where  $\epsilon^\infty$  is the electronic contribution to the dielectric tensor and the second term is the sum of the contributions from each polar phonon.  $\mu$  labels the phonon modes with fre-

TABLE II. Electronic and lattice contribution of the static dielectric constant for LAO/PTO and KSO/PTO superlattices.

	Electronic contribution		Lattice contribution	
	LAO/PTO	KSO/PTO	LAO/PTO	KSO/PTO
$\epsilon_{xx}$	6.39	5.93	137.19	90.12
$\epsilon_{yy}$	6.39	5.93	137.19	90.12
$\epsilon_{zz}$	6.14	5.34	43.09	24.99

quency  $\omega_\mu$ ,  $\bar{Z}_{\mu\alpha}^*$  is the mode effective charge corresponding to mode  $\mu$  in the Cartesian direction  $\alpha$  and  $\Omega_0$  is the volume of the primitive unit cell. The mode effective charge in the  $\alpha$  direction for a given mode  $\mu$  is related to the eigendisplacement  $U_\mu(\kappa\beta)$  involving ion  $\kappa$  and the Born effective charge tensor,  $Z^*$  by,

$$\bar{Z}_{\mu,\alpha}^* = \frac{\sum_{\kappa\beta} Z_{\kappa,\alpha\beta}^* U_\mu(\kappa\beta)}{\left[ \sum_{\kappa\beta} U_\mu^*(\kappa\beta) U_\mu(\kappa\beta) \right]^{1/2}}. \quad (2)$$

*Electronic dielectric constant.* The results for the electronic dielectric tensor are shown in Table II. The electronic contributions are of almost the same magnitude for LAO/PTO and KSO/PTO superlattices as expected from the similarity of their LDA band gaps.

*Lattice dielectric constant.* Our calculated lattice contributions to the dielectric tensor are listed in Table II. We find that the lattice contribution to the static dielectric constant is quite different between LAO/PTO and KSO/PTO superlattices. To understand the origin of the difference, we next carry out detailed analysis of the phonon frequencies and mode effective charges for the phonon modes which contribute to  $\epsilon_{zz}$ ; that is the relevant quantity for superlattices grown along the [001] direction with significant off-centric movements along the  $z$  axis. A large lattice dielectric response can be the result of the presence of one or more very low frequency polar phonons and/or anomalously large mode effective charges. Our analysis, as listed in Table III, shows that for the LAO/PTO superlattice, the lattice dielectric constant originates essentially from the dominant contribution of the lowest mode at  $115 \text{ cm}^{-1}$ ; this in turn arises from the combined effect of large mode effective charge and low frequency of the phonon mode. The contributions of different ions to the mode effective charge are found to be of comparable magnitudes.

In the case of the KSO/PTO superlattice, on the other hand, the dominant contributions come from more than one phonon mode. The major contributions arise from the phonon mode at  $209.94 \text{ cm}^{-1}$ , which has a giant mode effective charge, and that at  $125.83 \text{ cm}^{-1}$ , which has low frequency. The giant mode effective charge for the phonon mode at  $209.94 \text{ cm}^{-1}$  comes primarily from the  $\text{Ti}^{+4}$  and  $\text{Sb}^{+5}$  ions and the planar oxygens situated at the  $\text{SbO}_2$  layer. Thus, the temperature dependence of dielectric response of KSO/PTO superlattice is expected to be weaker than that of the LAO/PTO superlattice.

TABLE III. Phonon frequencies in  $\text{cm}^{-1}$ , corresponding mode effective charges in unit of  $|e|$  and the contribution to static dielectric constant.

LAO/PTO			KSO/PTO		
$\omega$	$\bar{Z}_{\mu,zz}^*$	$\epsilon_{\mu}^{zz}$	$\omega$	$\bar{Z}_{\mu,zz}^*$	$\epsilon_{\mu}^{zz}$
115.19	0.82	21.95	125.83	0.57	8.32
181.17	0.70	6.50	194.37	0.60	4.03
302.57	1.24	7.33	209.94	1.06	10.06
363.04	0.74	1.83	284.69	0.36	0.68
564.96	0.60	0.49	458.66	0.43	0.37
681.35	1.01	0.95	639.09	1.08	1.20
757.08	0.27	0.05	801.07	0.84	0.46

#### IV. SUMMARY

We have carried out a detailed computational study of superlattices formed out of alternating layers of one unit cell thick FE and PE components, considering several different  $\text{ABO}_3$  perovskites. We find that the tendency of the superlattices to exhibit polar properties depends strongly on the chemistry of the PE and FE components. In addition to interfacial polar discontinuities at the interfaces between the PE and FE layers, the epitaxial strain, rotational instability of the PE layer and the presence of  $d^0$  second-order Jahn-Teller active ions in the PE layer contribute to determining the polar behavior. While the polarization arising from a polar discontinuity is generally not switchable, other routes to polar behavior discussed here, do allow polarization switching.

The strongest polar response was found for superlattices with polar discontinuities and formed out of FE and  $d^0$  PE layers.

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